# Comparison of Boost Chopper and Active Buffer as Single to Three Phase Converter

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Abstract—This paper presents a comparison in terms of efficiency and volume between the single-to-three-phase power factor correction (PFC) converter. A conventional PFC circuit that consists of a boost chopper requires a large boost-up inductor and large smoothing capacitors to decouple the power ripple. The size and efficiency of the converter become a discussion issue recently. On the other hand, a single-to-threephase power converter using an active buffer has been proposed. The active buffer does not require a large inductor and large smoothing capacitors in the DC link part. These two types of converters are designed and simulated to calculate the losses. In addition, a prototype converter has been built and tested. The efficiency achieves 94.6% at 1.5-kW same as the calculated efficiency. Furthermore, the efficiency increases by 1.5% comparing to the conventional converter. In addition, the volume is decreased by approximately 0.7 times then the size of the conventional converter.

### I. INTRODUCTION

Single-phase to three-phase converters achieve energy saving in the application of home motor appliances. One of the important requirements of the converter is to provide low input current harmonics. Therefore many power factor correction (PFC) converters and control methods have been proposed [1]-[3]. At the same time, studies on the high efficiency and design of the volume are very important subjects in this field. The most common structure of PFC converter is the single-switch boost chopper circuit (conventional converter) as shown in Fig. 1 [1]. This circuit can control the input current easily. However, this converter requires a large boost-up inductor and a large smoothing capacitor to decouple the power ripple, which is a frequency twice of the power supply at the DC link part. In addition, the DC link voltage is always higher than the maximum input voltage because a boost-up converter is used. Therefore the switching loss of this conventional converter becomes high.

In order to reduce the volume of the smoothing capacitor, some power decoupling converters have been proposed [4], Jun-ichi Itoh Member, IEEE Nagaoka University of Technology 1603-1 Kamitomioka-machi Nagaoka City Niigata, Japan itoh@vos.nagaokaut.ac.jp

[5]. These circuits add the a few switching devises and energy buffer such as capacitor or reactor to the conventional boost chopper. Certainly, the voltage ripple in the DC part can be reduced by the control of the energy buffer even if the small something capacitor is used in DC part. However, the additional circuit for the power decupling causes increasing the power loss.

Apparently, a single-to-three-phase power converter with an active buffer (proposed converter) as shown in Fig. 2 has been proposed in [6] in terms of loss reduction of the power decoupling circuit. This converter is based on the concept of an indirect matrix converter that coupled with an active buffer to decouple the power ripple. The converter obtains sinusoidal waveforms on the input and output current. In addition, the size of the converter is reduced because the converter does not require a large smoothing capacitor and a large boost inductor in the DC link part. However, the clarifying of the efficiency and the volume are remained unidentified.

This paper demonstrates a comparison on the efficiency and the volume among these converters. At first, the paper discusses the circuit layout and control methods for these single-to-three-phase PFC converters. There are two type of boost up operation modes which are known as the continuous current mode (CCM) and the discontinuous current mode (DCM). Second, each parameter of the passive components is designed and utilized in the simulation analysis in order to compare the losses of these converters.



Fig.1 Conventional converter.

Then the size of the heat sink is calculated based on the simulation results. Nevertheless, a prototype of the proposed converter has been built and tested in order to validate the loss analysis. As a result, the efficiency of the proposed converter is 1.5 % higher than the conventional converter with DCM boost chopper. In addition, the total volume of the passive components is approximately decreased by 0.7 times comparing to the conventional converter with CCM boost chopper.

#### II. **CIRCUIT CHARACTERISTICS**

Figure 1 shows a single-to-three-phase converter with a single switch boost converter. The converter consists of a diode rectifier, inverter and boost chopper. There are many control methods can be applied into this PFC [1]-[3]. The point of the control method is as following.

- The current of an inductor is either CCM or DCM. •
- Duty ratio of the switch in boost chopper is either • constant or variable.
- Frequency of the switch in boost chopper is either constant or variable.

The simplest controls such as constant duty ratio, constant frequency or line frequency commutated control can obtain high power factor easily for low power applications. However, the input current remains distorted at low voltage boost ratio. On the other hand, advanced control strategies can control the input current into a clear sinusoidal waveform based on the duty ratio or switching frequency. In this paper, CCM or DCM operation with constant switching frequency and variable duty ratio methods are discussed.

Figure 2 shows a single-to-three-phase converter with an active buffer [6]. The active buffer that consists of a discharge circuit and a charge circuit replaces the boost chopper to decouple the power ripple, which the power ripple has a frequency that is twice of the power supply. The discharge circuit consists of a small capacitor and a switch. The charge circuit is similarly to a boost chopper circuit but using a smaller inductance value because the current is controlled based on DCM. The voltage ripple in the DC link part is absorbed to the small capacitor  $C_{dc}$  by controlling its terminal voltage. The terminal voltage of  $C_{dc}$  has large fluctuation according to the energy ripple which comes from the input side.

Figure 3 shows three different control method diagrams for PFC circuits. The switching duty ratio  $d_l$  of CCM is obtained by PI controller using the inductor current as shown figure 3 (a). In contrast, DCM can obtain the duty  $d_l$  using the equation without a current sensor as follows:

$$d_{l} = \sqrt{\frac{2L_{b}(v_{c} - v_{in})i_{l}^{*}}{v_{in}v_{c}T_{sw}}},$$
(1)

where,  $L_b$ ,  $v_c$ ,  $v_{in}$ ,  $i_l^*$  and  $T_{sw}$  are inductance of the boost-up inductor, DC link capacitor voltage, input voltage, inductor



(c) Proposed method

 $V_{C}$ 



current command and switching period of the switch in boost chopper, respectively.

Therefore, for both the conventional converters, the inductor current command  $i_l^*$  is obtained by a PI controller.

In the proposed control method, the power ripple is compensated by the discharge circuit and the charge circuit. The control method of the charge circuit is based on the DCM. Therefore the duty ratio is determined by (1). It should be note that the charge circuit and the discharge circuit are operating alternately at per quarter cycle of the power grid frequency. Thus, half of the input power is supplied directly to the inverter. Therefore the inductor current command  $i_l^*$  is calculated by

$$i_{l}^{*} = I_{lN} |\sin(\omega t)| - \frac{I_{lN}^{*}}{2|\sin(\omega t)|},$$
 (2)

where  $I_{IN}^{*}$  is the amplitude of the input current command and  $\omega$  is the input single phase angular frequency In addition, the capacitor voltage is fluctuating in this system. Hence, the power ripple  $W_C$  which is the electric storage energy is calculated by the maximum capacitor voltage  $V_{Cmax}$  and minimum capacitor voltage  $V_{Cmin}$ . Therefore  $I_{IN}^*$  can be expressed by

$$I_{IN}^{*} = \frac{2\omega W_{C}}{V_{IN}} = \frac{\omega C_{dc}}{V_{IN}} \left( V_{C \max}^{2} - V_{C \min}^{2} \right), \qquad (3)$$

where  $V_{IN}$  is the peak value of the input voltage,  $C_{dc}$  is capacitance of the DC link capacitor. Notice that the proposed circuit is not implemented with the PI controller, as a result, the transient response for the control of DC link voltage is fast and stable.

#### III. DESIGN OF PARAMETERS

This section explains a design example for a 1.5- kW class PFC converter. Table 1 provides the common specification of the converters.

# A. Input filter

The input filter for PFC circuit must have enough ripple attenuation at per switching frequency to satisfy the EMI requirement. In order to satisfy the above requirements, the cut-off frequency is required to be lesser than 1/5 to 1/10 times of the switching frequency. In this case, we design the cut-off frequency  $f_{cf}$  sets to 1.5 kHz. Also, in order to control the input power factor closed to unity at the line frequency, the reactance of input filter  $L_{in}$  is set to 1% of rated impedance of converter. From these specifications, we obtain

$$L_{in} = \frac{\% LZ_{cov}}{2\pi f_{in}} = \frac{0.01 \frac{200}{7.5}}{2 \cdot \pi \cdot 50} = 0.85 \, mH \,, \tag{4}$$

$$C_{in} = \frac{1}{L_{in} (2\pi f_{cf})^2} = \frac{1}{0.85 \cdot 10^{-3} (2\pi 10 \cdot 10^3)^2} = 13.2 \ \mu F$$
(5)

# B. Boost-up inductor $L_b$

This section discusses the design of the boost-up inductor. In order to simplify the derivation, we design the inductor value based on the peak value of the input voltage. At the input phase of  $\pi/2$ , the peak value input voltage is  $V_{IN}$  and the capacitor voltage is assumed as the average value  $V_C$ .

First of all, the ripple of the inductor current is discussed. The inductor current ripple  $\Delta I_L$  is obtained from

$$\Delta I_L = \frac{V_L}{L_b} \Delta t_{on} \,, \tag{6}$$

where  $\Delta t_{on}$  is turn on time of the switch in the boost chopper and  $V_L$  is inductor voltage of the boost-up inductor.  $V_L$  equals  $v_{in}$  when the switch is turned on. In contrast, when the switch is turned off,  $V_L$  equals to  $v_c$  minus  $v_{in}$ . Therefore, we obtain Eq. (7) at the maximum ripple of the inductor current.

$$0 = \frac{V_{IN}}{L_b} \Delta t_{on} - \frac{V_C - V_{IN}}{L_b} (T_{sw} - \Delta t_{on})$$

$$\Delta t_{on} = \frac{V_C - V_{IN}}{V_C} T_{sw}$$
(7)

Table 1 Common specification of converters.

Items	Value	Items		Value
Input voltage (rms)	200 V	Average capacitor voltage		350 V
Input frequency	50 Hz	Carrier frequency		10 kHz
Input filter L <sub>in</sub>	0.85 mH	Output power		1.5 kW
(% impedance)	1%	Output frequency		50 Hz
Input filter C <sub>in</sub>	13.2 μF	Tempera	Ambient	40 °C
(% impedance)	0.02 %	ture	Junction	125 °C



Fig.4 Definition of inductor current and capacitor voltage parameters.

From Eq. (6) and (7), the required inductance of the boost-up inductor  $L_b$  is obtained by

$$L_{b} = \frac{V_{IN}(V_{C} - V_{IN})}{2V_{C}I_{L}\Delta I_{L}f_{sw}} , \qquad (8)$$

where  $f_{sw}$  is the switching frequency of the chopper.

Here, the current ripple ratio  $r_l$  of the inductor, which is normalized by the peak value  $I_L$  of average inductor current for one switching period is expressed in Eq.(9).

$$r_l = \frac{\Delta I_L / 2}{I_L} \quad . \tag{9}$$

Therefore Eq. (8) can be rewritten as

$$L_{b} = \frac{V_{IN}(V_{C} - V_{IN})}{2V_{C}I_{L}r_{I}f_{sw}}$$
 (10)

The required inductance of the boost-up inductor  $L_b$  is dominant at the maximum inductance current  $I_L$  and the ratio of the inductor current ripple  $r_l$ . Note that in the inductor current, the ratio of the inductor current ripple  $r_l$  is from 0 to 1 means that the inductor current is a continuous current (CCM). Over than 1 means the inductor current is controlled as a discontinuous current (DCM). Then the peak values of the each current mode are calculated by

$$I_{L_peak} = I_L r_l + I_L \quad \text{, when} \quad r_l < 1 \text{ (CCM)} \\ I_{L_peak} = 2I_L r_l \quad \text{, when} \quad r_l \ge 1 \text{ (DCM)} \quad . \tag{11}$$

From (11),  $I_{L peak}$  of DCM becomes twice of the  $I_L$  and more.

In term of design, we assumed that the ripple ratio of inductor current  $r_l$  for CCM is lower than 0.1 p.u. For the comparisons,  $r_l$  parameter for the DCM and proposed converter needs to be 1.1 p.u. From the calculation, the boost-up inductor  $L_b$  is obtained as shown in Table 2. Notice that in the proposed circuit, the value of inductor current  $I_L$  is half of the conventional converters as shown in Eq. (2).

# C. DC capacitor $C_{dc}$

In the single-phase to three-phase converter, the electric storage energy required to compensate the power ripple  $W_C$ is obtained by

$$W_{C} = \frac{1}{2} V_{IN} I_{IN} \int_{0}^{\frac{1}{4f_{m}}} \sin(2\omega t) dt ,$$

$$= \frac{V_{IN} I_{IN}}{2\omega_{m}} ,$$
(12)

where  $I_{IN}$  is the amplitude of the input current and  $\omega_{In}$  is the input single phase angular frequency. Moreover, the  $W_C$  in the capacitor is required from the relations between the electric power and the capacitor voltage by (13).

$$W_{C} = \frac{1}{2} C V_{C \max}^{2} - \frac{1}{2} C V_{C \min}^{2}, \qquad (13)$$

where,  $V_{Cmax}$  is the maximum voltage, and  $V_{Cmin}$  is the minimum voltage of the buffer capacitor.

The electric storage energy used to compensate the power ripple  $W_C$  is obtained by (12) and (13). Therefore, the minimum capacitance in the buffer circuit is obtained by (14).

$$C_{dc} = \frac{2W_{C}}{V_{C_{\max}}^{2} - V_{C_{\min}}^{2}}$$

$$= \frac{V_{IN}I_{IN}}{\omega(V_{C_{\max}}^{2} - V_{C_{\min}}^{2})}$$
(14)

The capacitance  $C_{dc}$  is obtained from the ratio of the capacitor voltage ripple  $r_c$  which is expressed in (15). The capacitor voltage ripple  $r_c$  is normalized by the average value  $V_c$  of the capacitor voltage for a grid period.

$$r_c = \frac{\Delta V_C / 2}{V_C} \quad . \tag{15}$$

Accordingly, the capacitance  $C_{dc}$  is obtained from

$$C_{dc} = \frac{W_C}{\omega_{in}V_C^2 r_c} ,$$

$$= \frac{V_{IN}I_{IN}}{4\omega_{in}V_c^2 r_c} ,$$
(16)

Therefore the capacitance  $C_{dc}$  depends on the peak-peak voltage  $\Delta V_C$ .

In the conventional converters, the DC capacitor voltage must be sufficiently higher than the maximum input voltage to control the PI controller stable. Therefore, we assume the ratio of the capacitor voltage ripple  $r_c$  parameter is 2.5%. In

Table 2 Design value of parameters

Items		Proposed converter (CCM)		Conventional converter (DCM)
ctor	<i>r</i> <sub>l</sub> 1.1 p.u.		0.1 p.u.	1.1 p.u.
Boost Induc	$L_b$	0.46 mH	2.6 mH	0.23 mH
	$I_L$	5.3 A	10.6 A	10.6 A
	$I_{L_peak}$	11.7 A	11.7 A	23.3 A
DC-link cpapcitor	$r_c$	0.143 p.u.	0.025 p.u.	0.025 p.u.
	$\Delta V_C$	100 V	17.5 V	17.5 V
	$C_{dc}$	Required : 136 uF Selected : 150uF	Required : 136 uF Selected : 150uF	Required : 136 uF Selected : 150uF
	Rated ripple current	5A	5A	5A



between experiments and simulations.

the proposed converter, the fluctuation of the DC capacitor voltage can be controlled by the active buffer. Therefore the ratio of capacitor voltage ripple  $r_c$  parameter is set to 14.3%. So, requirements for capacitance  $C_{dc}$  of these converts are obtained as shown in Table 2. However, the selection of the electrolytic capacitor must consider upon its rated ripple current. Therefore, we select the closest capacitor that meet these conditions as shown in Table 2.

# IV. COMPARISON OF LOSSES

This chapter shows the loss analysis using the circuit simulator Piece-wise Linear Electrical Circuit Simulation (PLECS). We assume that each winding resistance of the inductor is same as  $0.25 \Omega$ . The motor condition is simulated by ideal current sources. Here, the rated voltage of the motor specification is generally 200 V. However, in the proposed converter, the voltage transfer ratio between the input voltage and the output voltage is less than 0.707 because the principle of the converter is a step-down converter. Therefore the motor rating for the proposed converter is changed to 141 V.

In order to validate the simulation results, the proposed converter has been tested practically. The experimental conditions are the same as the simulation, in Table 1 and 2. Figure 5 shows operation waveforms of the proposed converter. Sinusoidal waveforms are obtained on the single-phase input current and three-phase output current, with a single-phase power factor of over 99 %.

Figure 6 shows the comparison of the efficiency between experiments and simulations. The proposed system can achieve efficiency 94.6 % similar to the simulated loss analysis. Moreover, simulation results of the loss can achieve approximately the same efficiency to the experimental results at any range. That is, those experimental results confirmed that the power loss for each converter can be discussed based on loss simulations.

Figure 7 shows loss comparisons among the three converters. The total efficiency of the proposed converter is increased by 0.7 % comparing to the CCM. The largest difference shown in the loss is the boost inductor loss. DCM shows the largest in the boost inductor loss because the peak current is the highest among these converters. (Refer to Table 3). In the proposed converter, although the peak current is equal to CCM, the amount of current flows into the boost-up inductor is nearly quarter of the CCM.

Figure 8 shows a study on the losses among the boost choppers (conventional circuits) and the active buffer (proposed converter). The loss of the active buffer is decreased by 10 to 20 % in compared with the conventional boost choppers. In particular, even the number of switches is increased in the active buffer, but the current passing through the active buffer is quarter of the input current. Therefore the conduction loss is decreased.

#### V. DESIGN OF CONVERTER VOLUME

# A. Inductor

The design of the inductor volume can be calculated by using an area product method [7]. The area product  $A_p$  is defined as following

$$A_p = A_e A_w \,, \tag{17}$$

where  $A_e$  is the cross-sectional area of magnetic core,  $A_w$  is the cross-sectional area of the winding wire as shown Fig. 9. The area product  $A_p$  can obtain the volume due to bisect  $A_e$ and  $A_w$  at right angles. The volume of an inductor can be related to the area product  $A_p$ . The relationship is derived according to







Fig.9 Design of core.



$$V_{I} = K_{V} A_{n}^{\frac{3}{4}} , \qquad (18)$$

where  $K_V$  is a constant related to core configuration values.

The area product of an inductor is obtained as

$$A_p = \frac{2W_m}{K_u B_m J_w} , \qquad (19)$$

where  $W_m$ ,  $K_u$ ,  $B_m$  and  $J_w$  are the energy stored in the inductor, the utilization factor, amplitude of a magnetic flax density in the core, and the amplitude in the current density of the winding conductor, respectively.

We designed a magnetic ferrite C-core based on the following parameters as shown in Fig.9:  $K_v = 19.2$  (the rated A : B and C : D is set to 1:3),  $K_u = 0.5 B_m = 0.8$  T and  $J_w = 4$  A/mm<sup>2</sup>.

Figure 10 shows the relationship between the inductor volume and the area products. From (18), (19), the volume of an inductor is proportional to the three-quarters power of the stored energy in the inductor. In this specification, the volume of the boost inductor in the active buffer can be decreased by 70% lower than the standard boost chopper.

#### B. Heat sink

Heat sinks are designed by concerning about the power density. At first, we calculate the cooling system performance index (CSPI) [8],[9] as

$$CSPI = \frac{1}{R_{th}V_F}$$
 (20)

Figure 11 shows a simplified thermal model. Parameters of resistance  $R_{th_j-c}$  and  $R_{th_c-f}$  are obtained from the data sheet.  $R_{thf}$  is calculated from (20) with loss analysis data.

In this paper, the heat sink is designed to meet the following specifications: CSPI = 5, Junction temperature = 125 °C, ambient temperature = 40 °C.

# C. Capacitor

The design of the capacitor volume is difficult to indicate by mathematical expression. Therefore, the capacitor volume is designed based on the available market products.

Figure 12 presents three different types of capacitor that can be utilized as a DC capacitor. As can be seen in Fig. 12(a), the volume of these capacitors is proportional to the capacitance. The smallest capacitor for the proposed converter is shown in Fig. 12(a). Notice that the selection of the electrolytic capacitor must consider upon its rated ripple current. Therefore, the large capacitor of conventional converter must select in fig 12(b), and Fig. 12(c).

Figure 13 show the total volume of the passives components implemented in the conventional converters and the proposed converter. The total volume of the proposed converter is shown to decrease by 0.6 times in compared with the conventional converter. In particular, the volume of the active buffer, which includes of the boost inductor and the DC capacitor, can be reduced by approximately 60% than that of the standard boost chopper.

Table 3 shows the comparison among these converters. The efficiency of the proposed circuit is higher than the conventional circuits even the amounts of switches are increased in the proposed circuit. In addition, volume of the proposed converter is smaller than conventional circuits due to the decrement on the inductor size.

# VI. CONCLUSION

This paper compares the efficiency and the volume between several single-to-three-phase PFC converters. The efficiency of the proposed converter is highest efficiency and smallest volume of these converters. In particular, the proposed converter is 1.5% higher than the conventional converter with DCM. In addition, the total volume of the proposed converter is reduced by 0.7 times than that of the conventional converter with CCM. Therefore, the converter can achieve downsizing and high-efficiency by using the proposed active buffer.

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Table 3 Comparison of the conventional CCM, DCM and proposed converter.

	Proposed	Conventional converter		
	converter	ССМ	DCM	
Volume of converter size [cm <sup>3</sup> ]	$435\mathrm{cm}^3$	$654\mathrm{cm}^3$	547 cm <sup>3</sup>	
Volume of inductor size [cm <sup>3</sup> ]	$53.6  \mathrm{cm}^3$	196 cm <sup>3</sup>	89cm <sup>3</sup>	
Converter efficiency [%]	94.6 %	94.1%	93.1%	
The number of power devices	IGBT : 8 Diode : 5	IGBT : 7 Diode : 5	IGBT : 7 Diode : 5	
The number of necessary sensor	2	3	2	

XThis result calculated by Table 1 and 2 specifications.

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